Available Volume Fraction of Macromolecules in the Extravascular Space of a Fibrosarcoma: Implications for Drug Delivery

Ava Krol, Julie Maresca, Mark W. Dewhirst, and Fan Yuan

Departments of Biomedical Engineering [A. K., J. M., F. Y.] and Radiation Oncology [M. W. D.], Duke University, Durham, North Carolina 27708

ABSTRACT

Steric exclusion of molecules in the extravascular space of tissues can be quantified by the available volume fraction \(K_{AV}\). Despite its clinical importance, however, there is a paucity of data in the literature regarding the available volume fraction of macromolecules in the extravascular space of tumor tissues. In this study, we quantified \(K_{AV}\) of inulin, BSA, and dextran molecules of \(M_r 10,000–2,000,000\) in polymer gels and fibrosarcoma tissues. The measurement involved: (a) sectioning of gels or tumor tissues into thin slices (~600 \(\mu\)m) using a Vibratome, (b) \textit{ex vivo} incubation of the slices in solutions containing fluorescently labeled tracers, and (c) quantification of the equilibrium tracer concentrations in both slices and solutions. We found that \(K_{AV}\) in gels decreased monotonically when the \(M_r\) of dextran was increased from \(M_r 10,000\) to 2,000,000. However, \(K_{AV}\) in tumor tissues was insensitive to the molecular weight of dextran in the range between \(M_r 10,000\) and 40,000. There was a sharp decrease in \(K_{AV}\) from 0.28 ± 0.14 to 0.10 ± 0.06 when the molecular weight was increased from \(M_r 40,000\) to 70,000. In addition to the molecular weight dependence, \(K_{AV}\) was heterogeneous in tumors, with intertumoral difference being greater than intratumoral variation. The interstitial fluid space, which was quantified by \(K_{AV}\) of inulin, was 50% of the total tissue volume. These data indicate that the fraction of the extravascular volume in tumors that is accessible to large therapeutic agents is heterogeneous and depends on the size of agents.

INTRODUCTION

Interstitial structure is one of the major barriers to drug delivery in solid tumors (1). Drug delivery in the interstitial space is governed by various transport parameters, including the available volume fraction \(K_{AV}\). \(K_{AV}\) is defined as the volume fraction in the extravascular space of tissues that is accessible to therapeutic agents (2, 3). \(K_{AV}\) depends on physicochemical properties of agents (e.g., size and configuration) and volume fraction of cells as well as structure and composition of extracellular matrix (2, 4–10). An increase in \(K_{AV}\) would improve both local distribution and total accumulation of drugs in solid tumors. One strategy to increase \(K_{AV}\) is to digest extracellular matrix in tumors (7, 11). For instance, it has been shown that treatment of solid tumors with hyaluronidase improves drug accumulation in tumor tissues (12, 13).

Most \(K_{AV}\) data in the literature are from normal tissues (2, 7–9, 14–22). A few \(K_{AV}\) data from tumors are available (23–27), and most of them are associated with small molecules (e.g., Na\(^+\), Cl\(^-\), mannitol, and EDTA; Refs. 23–26). Therefore, the available volume fraction of macromolecules has been assumed to be unity in previous numerical simulations of drug delivery in solid tumors (28–30). In this study, we developed an \textit{ex vivo} assay for measuring \(K_{AV}\) of different macromolecules. Our results demonstrate that only a small fraction of the extravascular space in tumors is accessible to exogenous macromolecules. Therefore, the assumption of unity for \(K_{AV}\) may overestimate the total accumulation of macromolecular drugs in tumors.

MATERIALS AND METHODS

Tumor and Tracers

A rat fibrosarcoma (MCA-R) was used in the study. Tumor chunks (~1 mm in diameter) were transplanted s.c. into the right hind limb of 2-month-old female Fisher rats (weighing ~150 g; Ref. 31). When tumors reached 2 cm in diameter, rats were anesthetized with i.p. injection of pentobarbital (50 mg/kg body weight), and tumor tissues were removed and put immediately into a centrifuge tube on ice, which contained DMEM. Then a piece of tumor tissue was glued onto a specimen block and transferred to the stage of a Vibratome (model 3000; Technical Products International, St. Louis, MO) maintained at 4°C. The tissues were then sectioned into thin slices (600 \(\mu\)m thick), unless otherwise specified.

Tracers used in the study included various dextran molecules of \(M_r 10,000–2,000,000\), BSA, and inulin (Sigma Chemical Co., St. Louis, MO). Dextran and BSA were labeled with rhodamine, and inulin was labeled with FITC. The tracers were dissolved in PBS at concentrations of 0.1–1.0 mg/ml (pH 7).

Preparation of Gels

A polymer gel was prepared to mimic connective tissues. The preparation involved dissolving gelatin (2%) and chondroitin sulfate (1%) from bovine trachea powder in PBS containing 1% BSA. The gel was formed when the polymer solution was placed in the refrigerator. A piece of gel was glued onto a specimen block and sectioned at 4°C as described above. The thickness of the gel slices was 600 \(\mu\)m, unless otherwise specified.

Incubation Chamber

A polycarbonate chamber was constructed to study the effect of tissue swelling on the available volume fraction. The chamber was 800 \(\mu\)m thick and 4 mm in diameter. Both ends of the chamber were covered with polyethylene frits. Therefore, tracers could easily diffuse into the chamber, but the volume of the chamber was fixed. Tumor tissues were sectioned into 400-\(\mu\)m slices and cut into discs of 4-mm diameter. The discs were sandwiched between two nylon meshes (thickness, 200 \(\mu\)m; diameter, 4 mm) and placed into the chamber. Therefore, the total volume of the disc plus nylon meshes was equal to the volume of the chamber. The whole chamber was then incubated in tracer solutions.

Equilibrium Time Constant

The quantification of \(K_{AV}\) involved incubation of tissue slices in solutions of fluorescently labeled tracers and measurement of equilibrium concentrations of tracers in tissues \(C_t\) and solutions \(C_w\), respectively. The time constant for reaching the concentration equilibrium was estimated by \(2h^2/D\), where \(h\) is the slice thickness and \(D\) is the diffusion coefficient of tracers in tissues (obtained from Refs. 32 and 33). The prediction of the equilibrium time constant was consistent with experimental observations when the fluorescence intensity in tissues was quantified as a function of incubation time (data not shown). The same equation was also used to estimate the equilibrium time constant in the incubation of gels.

Calibration of the Concentration Measurement

Fluorescence intensities in tissues \(I_t\) and solutions \(I_w\) were quantified after the equilibrium of incubation was reached. We found that both \(I_t\) and \(I_w\) were linear functions of tracer concentration in solutions \(C_w\) (obtained from Refs. 32 and 33). The prediction of the time constant was consistent with experimental observations when the fluorescence intensity in tissues was quantified as a function of incubation time (data not shown). The same equation was also used to estimate the equilibrium time constant in the incubation of gels.
Quantification of $K_{AV}$

Tumor (or gel) slices were incubated in solutions of tracers in microcentrifuge tubes at 4°C for a time period longer than 2h/2D. During the incubation, the solutions were stirred by a shaker (Labquake; Barnstead/Thermolyne, Dubaue, IA). At the end of incubation, $K_{AV}$ was determined as the concentration ratio between tissues (or gels) and solutions ($C_{tissue}/C_{sol}$ or $C_{gel}/C_{sol}$). The procedures for the quantification of $C_{tissue}/C_{sol}$ and $C_{gel}/C_{sol}$ are as follows.

Quantification of $K_{AV}$ in Gels. After incubation of gel slices in a tracer solution, the slices were cut into 4-mm diameter discs, using a skin biopsy puncher, and transferred into plastic wells (0.6 mm in depth), which were glued on a glass microslide and filled with PBS. The wells were sealed with glass coverslips. The incubation solutions were transferred into separate wells with the same thickness. The fluorescence intensities in gel discs and the solutions were quantified via a fluorescence microscope (Axiovert 100; Zeiss, Thornwood, NY) equipped with the fluorescence filter sets for rhodamine and FITC (Omega Optical Inc., Brattleboro, VT) and a photomultiplier (model 9658B; Thorn EMI Electron Tubes, Rockaway, NJ). On the basis of the concentration calibration described above, the available volume fraction was calculated as follows:

$$K_{AV} = \frac{\Delta I_{gel}}{\Delta I_{sol}} \tag{A}$$

The quantification was performed within 2 min to minimize the amount of tracer release from gels.

Quantification of $K_{AV}$ in Tissues. Similar to the quantification of $K_{AV}$ in gels described above, tissue slices were incubated, cut, and transferred into the plastic wells containing PBS, and the fluorescence intensities in tissue discs and incubation solutions were quantified via the same fluorescence microscope workstation as in gel experiments. On the basis of the concentration calibration described above, $K_{AV}$ in tumor tissues was calculated as follows:

$$K_{AV} = a h_{sol} \frac{\Delta I_{t}}{\Delta I_{sol}} \tag{B}$$

where $a = k_{gel}/R$, which depended only on optical properties of tissues and the wavelength of the light. It was independent of tracers and the thickness of tissue slices, if $h_{t}$ was >800 μm.

To determine the value of $a$, we performed a separate experiment. Circular discs of tumor tissues were incubated in the solution of rhodamine-labeled dextran 10 or FITC-labeled inulin in centrifuge tubes. The number of discs ($n$) was 8, and the volume of the solution ($V$) was 200 μl. The size of discs was 7 mm in diameter ($d$) and 0.6 mm in thickness ($h$). The incubation solutions were stored, using 100-μm glass capillaries, both before ($\Delta I_{t}$) and at the equilibrium state ($\Delta I_{eq}$) of incubation, and the fluorescence intensities in capillaries were quantified using the fluorescence microscope workstation. On the basis of the mass balance of tracers in microcentrifuge tube, $K_{AV}$ could be determined as:

$$K_{AV} = \frac{4V}{\pi d^2 h n} \left( \frac{\Delta I_{gel}}{\Delta I_{sol}} - 1 \right) \tag{C}$$

At the end of incubation, three tissue discs and the solution were transferred into six different plastic wells, as described above, and the mean values of fluorescence intensities in three discs ([$\Delta I_{gel}$]) and solutions in three wells ([$\Delta I_{sol}$]) were quantified. Substituting ($\Delta I_{gel}$) and ($\Delta I_{sol}$) and $K_{AV}$ obtained from Eq. C into Eq. B, $a$ could be determined. We found that $a = 1.10 \pm 0.45 \text{ mm}^{-1}$ (mean ± SD, $n = 4$) for rhodamine-labeled dextran 10 and $a = 3.02 \pm 1.34 \text{ mm}^{-1}$ (mean ± SD, $n = 4$) for FITC-labeled inulin, where $n$ is the number of tumors.

Although both Eqs. B and C can be used to determine $K_{AV}$, a major disadvantage of the second method is that it requires a lot of tissue from a tumor. Consequently, it cannot be used to quantify $K_{AV}$ in small tumors and cannot reveal intratumoral variations in $K_{AV}$. Therefore, we used only the first method in the study, except for the determination of $a$.

The available volume fraction in the extravascular space of fibrosarcoma determined in this study could be larger than $K_{AV}$ in vivo because tracers could enter both interstitial and vascular spaces. However, the vascular space in vivo occupies <10% of the total tumor volume (35, 36), and blood vessels likely collapsed after tumor removal from animals. Therefore, the overestimation of $K_{AV}$ in this study would be significantly less than 10%.

Viability of Tumors

Viability of tumor tissues after incubation was estimated, based on the Live/Dead assay. The procedure was as follows. Tumor tissues were digested by Pronase in a solution of 900 μl of DMEM and 100 μl of Pronase (2%), for 1 h at 37°C. At the end of incubation, Pronase was removed through washing tissues in 1.5 ml of DMEM three times. Then, the tissue suspension was digested by collagenase in a solution of 800 μl of DMEM and 200 μl of collagenase (1%) for 4 h at 37°C. At the end of the incubation, the tissue suspension was washed twice in 10 ml of saline and stained with the Live/Dead fluorescent dyes (Molecular Probes, Eugene, OR) for 15 min. The numbers of red (dead) and green (viable) cells observed under a fluorescence microscope (Axiovert 100; Zeiss) were counted and compared.

Statistical Analysis

The Mann-Whitney $U$ and Wilcoxon signed rank tests were used to compare the differences between unpaired and paired groups, respectively, and the Kruskal-Wallis test was used when more than two groups were compared. Tests were considered significant if $P$s were <0.05.

RESULTS AND DISCUSSION

Available Volume Fraction

Molecular Weight Dependence. The available volume fraction of different tracers was quantified in tumor tissues (Fig. 1). We found that $K_{AV}$ was not reduced as the molecular weight of dextran molecules increased from 10,000 to 40,000, but it decreased significantly if the $M_r$ was >40,000 ($P < 0.01$; Fig. 1). The mechanisms of these results were not clear, but they were unlikely to be caused by polydispersity of dextran molecules. The reason is twofold. (a) Similar results have been observed in the study of microvascular permeability of proteins and polypeptides in tumors (37). These molecules were monodisperse, as demonstrated by SDS-PAGE analysis, but the permeability is independent of $M_r$ in the range between 25,000 and 45,000 and decreases significantly when $M_r$ is increased from 45,000 to 66,000 (37). (b) We quantified the available volume fraction in a polymer gel, using the same dextran molecules. We found that $K_{AV}$ decreased monotonically as the size of dextran molecules increased (Fig. 1). Therefore, mechanisms related to structures of extracellular matrix need to be investigated.
Structures of extracellular matrix have been studied in the bone and normal microvessels (38–42). These studies have demonstrated that the structure of extracellular matrix on endothelial cells (i.e., the glycocalyx; Refs. 38 and 39) or in canaluli (41) is not random. Fibers in the matrix are organized by albumin, which binds to glycosaminoglycan side chains of proteoglycans. These side chains form a regularly spaced lattice with the pore size of ~7 nm in diameter, the size of albumin (38, 41). Direct observations of proteoglycan structures by electron microscope have demonstrated that the distance between attachment sites of the side chains is tissue dependent (43, 44). It varies between 7 and 11 nm, except for that in the aorta, which is 17 nm (43, 44).

The proteoglycan structure discussed above might explain the significant decrease in the slope of $K_{AV}$ profile as the molecular weight of tracers was increased from $M_f$ 40,000 to 70,000 (Fig. 1) because concentrations of hyaluronic acid and chondroitin sulfate are found to be elevated in a variety of epithelial and mesenchymal tumors (45). To test this hypothesis, we prepared a polymer gel composed of 2% suspension of fibers fit well to the $K_{AV}$ data in polymer gels (10, 18), and we quantified $K_{AV}$ in gels (Fig. 1). We found that there was no significant change in the slope of $K_{AV}$ profile as the $M_f$ of tracers was increased from 10,000 to 70,000 (Fig. 1) and that the shape of the curve shown in Fig. 1 could not be changed by increasing the concentrations of both chondroitin sulfate and BSA to 5% or by removing BSA from gels (data not shown). The lack of an abrupt change in the slope indicated that there was no cutoff pore size in gels. These results were consistent with previous studies using other polymer gels: polyacrylamide (6, 10), and collagen (2), and hyaluronate (2). The discrepancy between $K_{AV}$ in gels and $K_{AV}$ in tumors is likely related to the orientation of fibers in matrices. Mathematical models of spheres in a random suspension of fibers fit well to the $K_{AV}$ data in polymer gels (10, 46–49). However, mathematical models of spheres in matrices with regular patterns of fiber orientation predict a cutoff pore size in gels (50). Molecules larger than the pore size will be excluded from matrices (50).

There was no significant difference in $K_{AV}$ between dextran 70 and BSA in tumors (Fig. 1). However, $K_{AV}$ of albumin was significantly higher than that of dextran 70 in gels ($P < 0.01$; Fig. 1). The difference between tumors and gels could be due to nonspecific binding of albumin to gelatin and chondroitin sulfate.

**Comparison with Previous Studies.** Few data on the available volume fraction of macromolecules in solid tumors are available in the literature. However, the available volume fraction of macromolecules has been studied extensively in normal tissues (2, 7–9, 14–22). In these studies, $K_{AV}$ of albumin ranged from 0.04 to 0.22 (15–20, 22), except for two extreme cases: $K_{AV}$ of albumin is $<0.01$ in cartilage (8) and averages 0.41 the umbilical cord (7). Therefore, the albumin results in the fibrosarcoma model (0.04–0.17) are within the range reported for normal tissues.

The molecular weight dependence of $K_{AV}$ has also been investigated in cartilage (8, 14) and umbilical cord (7, 9) using dextran and globular proteins. It has been found that $K_{AV}$ decreases monotonically in both tissues as the molecular size is increased.

**Interstitial Fluid Space and the Partition Coefficient.** Steric molecular exclusion in the extravascular space of tissues depends on structure of extracellular matrix and volume of the interstitial fluid space. The latter has been quantified in solid tumors, using Na$^+$, Cl$^-$, manitol, and EDTA (for review see Ref. 51). Inulin has also been used as a marker for the interstitial fluid space in normal (52) and tumor (27) tissues. These studies have demonstrated that there is no significant difference between inulin space and sodium (27) or manitol (52) space.

The ratio of available volume fractions between tracers and interstitial fluid is defined as the partition coefficient (3). To estimate the partition coefficient of dextran 10 in the fibrosarcoma, we quantified the available volume fraction of dextran 10 and inulin, respectively, in the same tumor. We found that the available volume fraction (mean ± SD) of dextran 10 (0.26 ± 0.09, n = 4) was about one-half of that of inulin (0.50 ± 0.11, n = 4). The difference was statistically significant ($P < 0.05$). These data suggested that the partition coefficient of dextran 10 was 0.52, i.e., 52% of the interstitial fluid space in the rat fibrosarcoma was available to dextran 10. The result of the available volume fraction of inulin is consistent with previous studies of fibrosarcomas (51). In these studies, the interstitial fluid space in fibrosarcomas varied between 0.33 and 0.60 (51).

**Heterogeneity.** The available volume fraction was heterogeneous both within a tumor and among different tumors (Fig. 2). We compared the available volume fraction of dextran 10 in different regions of a tumor and found that the coefficient of variation was between 14 and 30% (Fig. 2). However, if the mean values of the available volume fraction from each tumor were compared, the coefficient of variation was 45%. These data suggest that the difference in tissue structure is more significant between tumors than within a tumor.

The heterogeneity could be caused by variations in the volume fraction of cells and structures of extracellular matrix. For example, $K_{AV}$ of albumin in hyaluronate gels decreases exponentially as a function of hyaluronate concentration and reaches a plateau at a concentration of 25 mg/ml, and $K_{AV}$ decreases linearly in colla-

**Fig. 1.** The available volume fraction of dextran (1 and ○) and BSA (■ and ●) in fibrosarcomas (□ and ◆) and polymer gels (○ and ●). Data points, means of 24–35 measurements in six to eight fibrosarcomas (tumor) or means of 12 measurements in four different gel preparations (gel); bars, SD.

**Fig. 2.** The available volume fraction of dextran 10 in five different fibrosarcomas. ○, individual measurements of $K_{AV}$. In each tumor slice, measurements were performed at three different locations. The number of slices from one tumor varied between five and six.
causes nonuniform distribution of macromolecules. (1, 53). The heterogeneous extravasation is heterogeneous, and regions in which tumor vessels are impermeable to macromolecules exist (1, 53). Therefore, the concentration of tracers may be higher in the tumor tissues. The reason is twofold. (a) Extravasation in solid tumors is heterogeneous, and regions in which tumor vessels are impermeable to macromolecules exist (1, 53). The heterogeneous extravasation causes nonuniform distribution of macromolecules. (b) The interstitial fluid pressure is elevated in solid tumors (1). The pressure gradient may force extravasated macromolecules to move to the periphery of tumors. Therefore, the concentration of tracers may be higher in the periphery than at the center of tumors (1, 54). The third method for determining \( K_{AV} \) involves incubation of tissue slices ex vivo in solutions containing tracers of interest and measurement of equilibrium concentrations of tracers in both tissues and solutions (2, 7–9, 14–16, 18, 19, 21). The advantage of this method is that concentration equilibrium between tissues and solutions can be established reproducibly and the equilibrium time constant is predictable. However, several key issues regarding potential problems in the measurement still need to be addressed.

### Viability of Tumor Cells

The ex vivo incubation of tissue slices in solutions of fluorescently labeled tracers may cause cell death. Therefore, a viability test was performed in our study. Tissue slices were incubated in PBS at 4°C for 24 h, which was longer than any incubation time in the \( K_{AV} \) study. The fraction of viable cells in tissues was quantified both before and at the end of the incubation. Immediately before the incubation, the fraction of viable cells in tissues was \( \sim 89\% \). After a 24-h incubation, the fraction of viable cells was \( \sim 90\% \). Therefore, the effect of incubation on cell viability could be neglected.

### Effect of Tracer Concentration

Measurements of \( K_{AV} \) might be affected by the concentration of tracers. We found that \( K_{AV} \) of both dextran 70 and BSA at the concentration of 0.1 mg/ml were not statistically different from those at 1.0 mg/ml (Fig. 3). However, both \( K_{AVs} \) were increased significantly if the concentration was 10 mg/ml (Fig. 3). There are two possible explanations for the data in Fig. 3. The first is aggregation of tracers in tissues, although no aggregation was observed in solutions. The second is the nonlinear partitioning phenomenon (55). Both theoretical and experimental studies have demonstrated that the partitioning of molecules between porous media and exterior solutions increases with the concentration of solutions, if the concentration is higher than a threshold level (55). To avoid the concentration effect on \( K_{AV} \), we always used a tracer concentration of \(< 1.0 \text{ mg/ml} \) in our experiments.

### Effect of Tissue Swelling

One of the major concerns associated with the ex vivo incubation of tissues is the change in structure due to swelling (7, 11, 56). The fibrosarcoma tissue swelled in physiological saline. We found that the weight of tissue increased 2.6 ± 2.0% (mean ± SD, \( n = 6 \)) during the first hour of incubation and that there was no significant change in the weight from 1 to 6 h (\( P = 0.26 \)). The weight increase was 7.2 ± 3.2% (mean ± SD, \( n = 6 \)) after 24 h of incubation.

The swelling may change the available volume fraction of macromolecules (9, 57). Therefore, minimizing tissue swelling will reduce error in measurements. In general, tissue swelling can be caused by (a) swelling of cells (58) and/or (b) swelling of extracellular matrix (7, 11, 56, 59–61). The former can be minimized using isotonic solutions, whereas the latter can be controlled using several methods. The swelling of extracellular matrix is predominantly caused by the Gibbs–Donnan osmotic pressure of proteoglycans because treatment of tissues with hyaluronidase results in de-swelling of preswelled tissues (7, 11). Swelling of extracellular matrix can be minimized by using hypertonic solutions (11, 56, 59–61) or supplementing incubation medium with polybase (e.g., polylysine; Ref. 11). However, the swelling still need to be addressed.
cross-link of proteoglycans by polylysine molecules reduces the available volume fraction. Another promising method for reducing tissue swelling without significantly disturbing its structures is to place tissue in a chamber with a fixed volume (9, 18). In doing so, tissue swelling effect on $K_{AV}$ can be controlled within 10% (18). To investigate the effect of tissue swelling on the quantification of the available volume fraction, we constructed a polycarbonate chamber described in the “Materials and Methods.” Tumor tissues were sectioned into 400-μm slices and cut into 4-mm discs. The discs were divided into two groups. In one group, three discs were placed in different chambers and incubated in tracer solutions. In another group, three discs were incubated freely in the same solutions. In each solution, discs were incubated for a time period longer than the equilibrium time constant. At the end of incubation, the available volume fractions of tracers were quantified and compared between two groups (Fig. 4). We found that the effect of tissue swelling on $K_{AV}$ was less significant than that of molecular weight. There was no statistical difference between the groups (Wilcoxon signed rank test). Therefore, tumor tissues were incubated freely in most of our experiments.

**Implications for Drug Delivery to Solid Tumors**

Novel therapeutic agents have been developed to target specific molecules in tumor cells. These so-called molecular medicines are more specific to tumor cells in comparison with conventional drugs. However, delivery of molecular medicines to tumor cells is a critical problem because these agents are, in general, macromolecules or nanoparticles (62, 63). Transport and accumulation of macromolecules or nanoparticles in tumors are limited by various factors, including microvascular permeability (37), interstitial diffusion coefficient (32, 33), and available volume fraction. To understand how the available volume fraction affects drug accumulation in tumors, we performed a pharmacokinetic analysis, using a compartmental model. The major assumption of the model was that the tumor compartment was well mixed, i.e., the concentration of drugs in the extravascular space was uniform. Thus, the governing equation is:

$$\frac{dC}{dt} = \frac{P}{V}(C_p - C/K_{AV}) \quad (D)$$

where $C$ and $C_p$ are the concentrations in the tissue and the plasma, respectively; $V$ is the total volume of tumor; $P$ is the microvascular permeability; and $S$ is the total surface area of vessels. In addition, we assumed that the transport in solid tumors would not affect significantly the plasma clearance of drugs. Therefore, the plasma concentration of macromolecules could be approximated by a biexponential function of time (28–30):

$$C_p = C_{p0}[\rho e^{-\lambda_1 t} + (1 - \rho)e^{-\lambda_2 t}] \quad (E)$$

where $C_{p0}$ is the initial value of $C_p$, $\rho$, $\lambda_1$, and $\lambda_2$ are constants. Eqs. D and E were solved analytically to obtain the concentration of drugs in tumors:

$$\frac{C}{C_{p0}} = \lambda_3^{-1} \ln \left[ \frac{\lambda_3 - \lambda_1}{\lambda_1 - \lambda_2} \left( e^{-\lambda_1 t} - e^{-\lambda_2 t} \right) + \frac{1 - \rho}{\lambda_3 - \lambda_2} \left( e^{-\lambda_3 t} - e^{-\lambda_2 t} \right) \right] \quad (F)$$

where $\lambda_3 = \frac{PS}{VK_{AV}}$ is the rate of drug transport from the plasma into the extravascular space of tumors. The drug accumulation in tumors, i.e., the percentage of the injected dose per gram of tissue, is proportional to $CI/C_{p0}$. The baseline values of $K_{AV}$, $PS/V$, $\rho$, $\lambda_1$, and $\lambda_2$ were chosen to be 0.2, $7 \times 10^{-5}$ s$^{-1}$, 0.3, $2 \times 10^{-4}$ s$^{-1}$, and $7 \times 10^{-6}$ s$^{-1}$, respectively. These values were close to those used in the study of antibody transport in solid tumors (29, 30). The simulation, using Eq. F and the baseline values of constants, indicated that $CI/C_{p0}$ was nearly a linear function of $K_{AV}$ at times longer than 24 h ($r^2 > 0.999$; Fig. 5). At 24, 48, and 72 h, the slopes of curves were 0.424, 0.232, and 0.127, respectively. However, these curves may become nonlinear if the baseline values are changed. The implication of the simulation is twofold. (a) Drug accumulation in tumors depends significantly on $K_{AV}$. Therefore, one strategy to improve drug delivery to tumors is to increase $K_{AV}$. (b) Steric molecular exclusion in tumors has to be considered in pharmacokinetic analysis of drugs. Assuming $K_{AV} = 1$ can cause a significant overestimation of drug accumulation in tumors, especially when drugs are macromolecules or nanoparticles.

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