PERSPECTIVE

The relationship between tumor blood flow, angiogenesis, tumor hypoxia, and aerobic glycolysis

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Abstract

Anti-angiogenic therapies are being pursued as means of starving tumors of their energy supply. While numerous studies show that such therapies render tumors hypoxic, just as many studies have, surprisingly, shown improved tumor oxygenation. These contradicting findings challenge both the original rationale for anti-angiogenic therapy and our understanding of the physiology of tissue oxygenation.

The flow-diffusion equation, which describes the relation between blood flow and the extraction of freely diffusible molecules in tissue, was recently extended to take the heterogeneity of capillary transit times (CTH) into account. CTH is likely to be high in the chaotic microvasculature of a tumor, increasing the effective shunting of blood through its capillary bed.

We review the properties of the extended flow-diffusion equation in tumor tissue. Elevated CTH reduces the extraction of oxygen, glucose, and cytotoxic molecules. The extent to which their net extraction is improved by anti-angiogenic therapy in turn, depends on the extent to which CTH is normalized by the treatment. The extraction of oxygen and glucose are affected to different extents by elevated CTH, and the degree of aerobic glycolysis - known as the Warburg effect - is thus predicted to represent an adaptation to the CTH of the local microvasculature.

Keywords: Angiogenesis, hypoxia, microcirculation, tumor blood flow, tumor metabolism, Warburg effect, tumor imaging.
Introduction

The survival of cancer cells is contingent on their supply of oxygen and nutrients such as glucose via the blood-stream. The establishment and growth of malignant tumors are, therefore, critically dependent on their ability to stimulate the formation of new blood vessels (angiogenesis) to support their metabolic needs (1). During the past decades, anti-angiogenic therapies have been pursued as a means of inhibiting tumor growth (2). Such therapeutic oxygen deprivation might be expected to have unwanted side-effects if unsuccessful: cancer cells become more aggressive, more resistant to chemo- and radiation-therapy, and more likely to metastasize under hypoxic conditions (3). Surprisingly, anti-angiogenic drugs have since been proven to have modest effect on tumor growth when administered alone (4, 5), but to be efficacious in combination with both chemotherapy and irradiation (6, 7) – even beyond an additive effect of the combined treatments (8). This has led to the hypothesis that anti-angiogenic drugs prune the chaotic tumor microvasculature to provide a more even distribution of blood and anti-cancer drugs across tumors, thereby improving tissue oxygenation and drug-responses (9). In support of this notion, experimental studies have demonstrated that anti-angiogenic treatment is followed by a 'vascular normalization window', during which microvascular density, length, diameter, and tortuosity are reduced, capillary pericyte coverage is increased, and the basement membrane thickness and capillary permeability to plasma-proteins normalized (7, 10). In some studies, these changes are paralleled by increased tumor oxygenation and sensitivity to radiation and cytotoxic therapy are significantly increased (7, 10). This is not a consistent finding, however, in that as many studies have shown angiogenesis inhibitors to reduce tumor oxygenation (8, 11).

The finding that reductions in tumor microvascular density can improve tumor oxygenation and the delivery of small molecules to tumor tissue contradicts not only the original rationale for anti-angiogenic therapy, but also appears to contradict fundamental principles of physiology and
pharmacokinetics. According to these, the extraction of diffusible molecules, including oxygen and pharmaceuticals, always decrease if capillary surface area is reduced for a given tumor blood flow. The cause of this paradox must therefore lie in profound, therapy-related changes in either tumor blood supply, or in the extraction of solutes by the tumors.

The blood flow and oxygenation is well-characterized in several tumor types (12-15). Most tumors display considerable variability in tumor blood flow (TBF, mL blood/mL tissue/minute), both within and among tumors of a given type, with TBF ranging from near-zero to several times that of the surrounding, normal tissue (12, 16). The oxygen extraction fraction (OEF) in tumor tissue is generally poor, ranging from only 5% to 50% of the incoming arterial blood's total oxygen content (12). Most often, blood flow and low oxygen extraction combine to a low availability of oxygen in tumors, as evidenced by oxygen tensions that are generally lower than those of surrounding tissue (12-16). The incomplete extraction of oxygen by tumors with low tissue oxygen tension is characterized as diffusion-limited or chronic hypoxia to indicate that oxygen diffusion from blood tissue must somehow be hindered (16). In some tumors, blood is constantly redistributed across tumor parts ('cycling'), resulting in what has been dubbed flow limited or acute hypoxia (16).

Chronic hypoxia is traditionally ascribed to increased diffusion distances from capillaries to cells within the chaotic tumor microvasculature, causing cells far from capillaries to receive less oxygen than required (16). This notion is difficult to reconcile with the finding that tumor oxygenation in many cases improves as a result of anti-angiogenic treatment, during which average inter-capillary distances invariably increase. A more recent hypothesis of chronic tumor hypoxia states that the microvasculature tends to develop functional arteriovenous shunts in the absence of the normal signaling of metabolic needs among microvessels (17). If vascular normalization restored normal signaling, such shunting might be reduced, the distribution of blood across the microvasculature improved, and oxygen extraction thereby increased (18).
We recently developed a model of the extraction of oxygen and other freely diffusible substances in tissue. The model extends the traditional flow-diffusion equation (19) to take not only blood flow into account, but also the effective shunting that occurs as some blood flows along capillary paths with limited oxygen extraction (20). In this review, we briefly describe the model and then examine its prediction with regards to the net extraction of oxygen, glucose and cytotoxic molecules under the assumption that tumor angiogenesis is accompanied by increased capillary transit time heterogeneity (CTH) – See figure 1. The model predicts that reduced extraction of oxygen, glucose, and cytotoxic molecules is a feature of elevated CTH, and thus of the formation of chaotic tumor vessels. Vascular normalization is predicted to improve tumor oxygenation and the extraction of cytotoxic molecules only when capillary hemodynamics is normalized (CTH reduced) as a result of the anti-angiogenic therapy. Meanwhile, therapeutic elevation of TBF is predicted to improve tumor oxygenation only in cases when CTH is moderately elevated. Lastly, increased CTH favors the extraction of glucose over oxygen. The degree of aerobic glycolysis - known as the Warburg effect (21) – in tumors is thus predicted to reflect the differential extraction of glucose and oxygen with increasing CTH as a result of tumor angiogenesis.

The relation between tumor blood flow and the extraction of diffusible substances: The overlooked importance of capillary transit time heterogeneity.

The relation TBF and the amount of freely diffusible molecules that can be extracted by tumor tissue is derived from the so-called flow-diffusion equation (19). The equation accurately describes the extraction of freely diffusible substances from a single capillary perfused at a given blood velocity. Replacing capillary flow velocity by tissue blood flow, this equation is now widely used to model the net extraction of freely diffusible substance in tissue, given the net capillary surface area per unit tissue volume, and their permeability to the substance (19). Figure 1 shows why this generalization from single capillaries to tissue is a gross oversimplification: According to the
experimentally proven single-capillary version of the flow-diffusion equation, any degree of capillary flow heterogeneity in tissue is bound to reduce the availability of a diffusible substance in tissue relative to the predictions of the universally applied ‘tissue version’ of this fundamental equation (22). Tumor vessels are highly tortuous and display profound changes in capillary wall morphology and blood cell adhesion (12). Such vascular changes, and possibly increases in local interstitial pressure, have been shown to disturb the distribution of capillary transit times in the tumor tissue. The image inserts are reproduced from elegant experiments performed by Quarles and Schmainda and show elevated transit time heterogeneity in a brain tumor model (23). As illustrated by Figure 2B, angiogenesis tends to lower the efficacy of oxygen extraction by effectively shunting oxygenated blood through the tumor microcirculation. Similarly, the oxygenation response to the removal of some of the capillary paths in Figure 2B by anti-angiogenic therapy is inherently difficult to predict. Below, we describe a general framework for estimating tumor oxygenation based on capillary transit time patterns such as those shown in Figure 2C, and demonstrate how treatment-related changes in capillary transit time patterns can be utilized to predict parallel changes in the net oxygenation of individual tumors, cf. Figure 2D.

**An extended flow-diffusion equation**

We recently extended the flow-diffusion equation to take the effects of CTH into account. The model is described in detail elsewhere (20) and summarized only briefly here. The model assumes a gamma variate distribution of capillary transit times in tissue (24), permitting us to characterize regional tumor hemodynamics by two parameters: The mean transit time (MTT) of blood through the capillaries, and CTH, which for the gamma variate equals the standard deviation of capillary transit times. The MTT is related to TBF and capillary blood volume (CBV - mL blood / mL tissue) through the central volume theorem, MTT= CBV/TBF (25). The maximum achievable extraction fraction ($\text{EF}_{\text{max}}$) for a diffusible substance with bidirectional clearance constant $k$ (in sec$^{-1}$) and a
given tissue concentration of the substances can then be determined by integrating over all transit
times of the respective capillaries. By doing so, the original flow-diffusion equation is only applied
to ensembles of capillaries with identical transit times, thereby avoiding the heterogeneity bias
shown in Figure 1. The resulting $E_{\text{Fmax}}$ for a given diffusible substance now depends on TBF, CBV,
CTH, the capillary permeability $k$ of the substance, and its tissue concentration.

Hemodynamic limitations to the extraction fractions of oxygen, glucose, and diffusible
molecules in tumors

Figure 3A shows a contour plot of the maximum extraction fractions for oxygen ($OEF_{\text{max}}$) as a
function of the MTT and CTH using the hemodynamics of a xenografted human breast carcinoma
as an example. The model was calibrated to the metabolic rates and TBF values reported by
Kallinowski et al (26) – see figure legend. Note that increases in CTH reduce the tumor’s ability to
extract oxygen for a given tissue oxygen tension. This effect is caused by the increased proportion
of blood that passes through the microvasculature too fast to permit proper extraction of diffusible
substances as CTH increases for a fixed TBF. CTH reduces the effective capillary surface area
available for diffusion for any diffusible substance (including pharmaceuticals) according to the
expression $PS = -TBF \cdot \ln(1 - E_{\text{Fmax}})$, where PS denotes the effective capillary permeability-surface
area product for the substance and $E_{\text{Fmax}}$ is determined by the extended flow-diffusion equation
(20).

The tumor’s microcirculation is highly chaotic, owing to the aberrant topology, morphology and
patency of newly formed microvessels, the increased vascular permeability and pressure from
surrounding fluids and tissue cells, and altered blood rheology (12). Tumor angiogenesis is
therefore expected to increase CTH as shown by the insert in Figure 1, and indicated by the arrows
in Figure 3A. As indicated by the vertical components of the arrows in Figure 3A, an increase in
CTH caused by angiogenesis can result in a significant reduction in $OEF_{\text{max}}$ for a given TBF and
tissue oxygen tension. This is consistent with the general finding of lower oxygen extraction fractions in tumors than in their host tissue (12). Also note that TBF is predicted to be a poor predictor of tumor oxygenation without simultaneous knowledge of CTH. By definition, angiogenesis increases the capillary blood volume. Meanwhile, the tumor expands, and the net capillary blood volume per unit tumor volume may therefore either increase, decrease, or remain constant. Note, however, that unless TBF increases in proportion to CBV, then MTT (equal to CBV/TBF), increases. The two cases of either reduced or prolonged MTT are indicated by the horizontal components of the two arrows in Figure 3A.

The net extraction of diffusible molecules

The upper limit imposed by the tumor’s microcirculation on the local metabolic rate of glucose, TMRglc$^{max}$, and oxygen, TMRO$_2$$^{max}$, can now be determined by multiplying their $E_F^{max}$ values by TBF and the arterial concentrations of glucose and oxygen, respectively. Figure 3B shows a surprising feature of high CTH: as indicated by the red arrow, increased TBF, without a concomitant reduction in CTH, can lead to a hemodynamic state (value of MTT and CTH) in which the availability of oxygen is unaltered or even reduced in comparison to the initial hemodynamic state. We refer to this critical level of shunting as malignant CTH and note that it is specific to the diffusion properties of the molecule and its tissue concentration (20). Figure 3B thereby encapsulates the requirements for angiogenesis to subserve the supply of nutrients to a tumor: While the formation of new vessels is clearly necessary to maintain sufficient vascularization (high CBV) and blood flow (TBF) in a given tissue volume, the chaotic nature of newly tumor vessels (and thus the high CTH) is a crucial limitation to the net amount of nutrients that can be extracted from the new vasculature.

The model predicts that strategies to improve tumor oxygenation by increasing TBF may prove unsuccessful unless the tumor’s microcirculation permits CTH to decrease in response to the
increased flow rate - See the oblique arrow in Figure 3B. Similarly, the model predicts that anti-angiogenic treatment can improve tumor oxygenation, and the extraction of cytotoxic molecules, by reducing CTH. While CTH has been shown to decrease in response to one anti-angiogenic agent, cf. Figure 2C, the schematic drawing in Figure 2B illustrates that tumor oxygenation responses are likely to depend critically on the way in which the microvascular ‘pruning’ affects the shunting of oxygenated blood. As illustrated by Figure 2D, this uncertainty may explain the variability of tumor oxygenation changes after anti-angiogenic therapy (8, 11), and may suggest measurements of CTH and MTT responses to anti-angiogenic therapy across tumors as means of understanding these oxygenation responses.

Aerobic Glycolysis

The iso-contour plot in Figure 3C. shows the net oxygen:glucose extraction ratio (OGR). Oxidative phosphorylation of glucose (complete breakdown of glucose to ATP) requires oxygen to be present in a ratio of approximately 5-6:1, while a relative lack of oxygen will result in the conversion of some glucose into lactate instead - glycolysis. Note that the differential extraction of glucose and oxygen results in a close dependency of OGR upon MTT and CTH. The anticipated changes in tumor hemodynamics as a result of angiogenesis (cf. insert in Figure 1) thus implies that tissue will have relatively easier access to glucose than to oxygen in tumors with a more chaotic microcirculation. The term 'aerobic glycolysis' was originally coined by Otto Warburg (21) who detected the phenomenon in tumor cells in vitro. This phenomenon, and its relation to other cancer traits (27), could in theory reflect cellular adaptations to the prevalent nutrients permitted by the tumor’s microcirculation.

Poor oxygen extraction from a chaotic tumor microcirculation: The role of tumor hypoxia.
The elevated CTH of tumor vasculature reduces the extraction of oxygen for a fixed tissue oxygen tension, cf. Figure 3A. The tumor's oxidative metabolism constantly metabolizes oxygen, and as the extraction of oxygen becomes limited by elevated CTH, this consumption therefore tends to reduce tissue oxygen tension. Consequently, blood-tissue oxygen concentration gradient - and thereby $\text{OEF}^{\text{max}}$ - increases. Figure 3D illustrates how tumor hypoxia permits the tumor to cover its oxygen needs, even if CTH continues to increase during angiogenesis: The green surface corresponds to combinations of MTT, CTH, and tumor oxygen tension, for which oxygen availability precisely matches the $\text{MRO}_2$ of the xenografted breast carcinoma used for illustration in Figures 3A-C ($\text{TMRO}_2 = 1.18 \text{ mL/100mL/min}$ according to ref (26)). The bell-shaped interior of surface therefore represents combinations of MTT, CTH and tumor oxygen tension for which the metabolic needs of this tumor type can be met. The red plane marks the boundary of malignant CTH, to the left of which increased tumor blood flow would reduce tissue oxygen availability. The label $a$ shows the theoretical maximum for the increase in CTH (indicated by a broken line parallel to the MTT axis) that can be sustained by tumor tissue at a tissue oxygen tension ($\text{P}_{\text{O}_2}$) level of 15 mmHg. Assuming for a moment that CTH increases while CBV (the capillary blood volume per tissue volume) remains constant during tumor angiogenesis, then CTH ultimately reaches a critical limit (Label $b$), where oxygen tension cannot be reduced further. At this time, the tumor effectively outgrows its vasculature, and necrosis is predicted to ensue. Note that MTT increases by a factor of 2 as CTH increases between condition $a$ and $b$, that is, TBF is reduced by a factor of 2. As CTH increases for a fixed CBV, the metabolic needs of the tumor can therefore be met by reducing TBF to ensure a higher oxygen extraction. This is consistent with the general finding of lower TBF in tumors than in their host tissue (12).

Discussion
The tendency of the tumor microcirculation to lose normal hemodynamic control has been described and modeled in detail by Pries and colleagues (17, 18), who also coined the associated ‘shunt problem’: Poor extraction of oxygen, glucose, and pharmaceuticals in tumors as blood is effectively shunted through capillaries with poorly controlled flow (18). The extent to which the extraction of diffusible substances is reduced by the loss of normal hemodynamic control across the capillary bed can be addressed by advanced simulation models of the microcirculation (17, 18). The extended flow-diffusion model (20), in its current form, does not account for non-uniform substance concentrations and spatial diffusion properties at the microscopic level – See discussion in Ref. (20). By these simplifications, it permits us to address salient features of the shunt problem for oxygen, glucose, and freely diffusible pharmaceuticals, based on tumor MTT (or blood flow) and CTH. Both these parameters can be derived from the retention of intravascular contrast agents in the tumor vasculature as observed by dynamic magnetic resonance imaging, computerized tomography, or contrast enhanced ultrasound (23, 28-30), as exemplified in Figures 1 (insert) and 2C. In principle, these techniques can therefore be applied in human malignancies in relation to therapies that target the tumor microvasculature. In preclinical models, intravital optical imaging techniques (10) provide additional means to achieve this information.

We propose that MTT and CTH estimates may predict the oxygenation status of tumors, their metabolic status in terms of ATP yields from mixed oxidative phosphorylation and glycolysis (27), and their uptake of freely diffusible molecules. Our analysis of MTT and CTH data obtained in an experimental tumor model shows that CTH can be normalized in part by anti-angiogenic therapy (23), but further suggests that the change in tumor oxygenation depends on parallel changes in MTT, cf. Figure 2D. While these findings reemphasize the need to understand tumor angiogenesis and hemodynamic control (17, 18), they also suggest that existing diagnostic imaging techniques
can be used to identify hemodynamic impairments of tumor oxygenation in relation to individualized cancer therapy.

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References


**Figure legends**

**Figure 1. The flow-diffusion relation for oxygen**

The classical flow-diffusion equation shows the maximum amount of oxygen that can diffuse from a single capillary into tissue, for a given flow velocity. In the graph, flow velocity and oxygen extraction for a single capillary are replaced by blood flow per volume unit (TBF) and net oxygen extraction per tissue volume (TMRO$_2^{max}$) on the x- and y-axis, respectively. This generalization is only true if all capillary flow velocities are identical. This is most easily understood by observing that net tissue oxygen availability is lower in case B (half of the capillaries have low flow, the other half high flows) than in case A (equal flows) although TBF is identical in the two cases: In the heterogeneous case (B), the net tissue oxygen availability is the average of the oxygen availabilities for the two flows, labeled $b$ in the plot. Owing to the concave shape of the TBF - TMRO$_2^{max}$ relation, which holds for capillaries with identical flows, $b$ is always smaller than $a$, the oxygen availability for homogenous capillary flows. Sources of poor microcirculatory control across the tumor microvasculature are discussed in detail in ref. (18). Note that several properties of individual tumor capillaries, blood rheology, and tumor microenvironment, can hinder a uniform distribution of erythrocytes. These include low-grade inflammation that increase the adhesion among capillary endothelium and blood cells (indicated by the rugged inner surface of the lower capillary), slow-passing white blood cells, capillary walls with abnormal surface properties and diameters, and capillary compression due to increased interstitial pressure in the tumor. Upstream vasodilation may
in fact amplify the redistribution losses shown above, as erythrocytes are forced through other branches at very high speeds, with negligible net oxygenation gains.

The image insert and the accompanying graph in the lower right of the figure show experimental evidence of the broadening of the distribution of capillary transit time distribution in a 9L rat brain tumor model from work by Quarles and Schmainda (23): While the distribution of transit times is relatively narrow in normal brain tissue, it is much broadened and CTH thereby elevated in the tumor rim, suggestive of angiogenesis as evidenced by their observations of increased capillary blood volume (23). Within the edema/tumor core, the transit time distribution is even broader and CTH more elevated.

Abbreviations: tumor blood flow (TBF); maximum tumor metabolic rate of oxygen (TMRO$_2^{\text{max}}$); capillary transit time heterogeneity (CTH)

**Figure 2. Effective shunting of oxygenated blood in capillary networks with heterogeneous, poorly regulated flow velocities.**

Panel 2A illustrates how capillary flow velocities in normal tissue are regulated to provide efficient extraction of oxygen. Red indicates fully oxygenated blood while the transition over orange and yellow to blue indicates gradual deoxygenation. In tumors (panel B), tight control of capillary flow distributions is invariably lost owing to factors such as the lack of normal, contractile pericytes on capillaries, irregular luminal capillary diameters, capillary compression by tumor edema, increased blood cell adhesion to the endothelium, and loss of the conducted vasomotor responses that ensure appropriate blood distribution in normal microvessels (18). The oxygenation response to the removal of specific capillary paths by anti-angiogenic therapy in this example depends critically on the resulting redistribution of capillary flows and changes in TBF – estimated here by the capillary transit time heterogeneity CTH and mean transit time MTT parameters.
Panel 2C shows the effects of two different doses of an anti-angiogenic agent, SU11657, on the distribution of transit times as recorded by Quarles and Schmainda (23). Note how the highest dose almost normalizes distribution of transit times compared to that of normal brain tissue. According to Figure 1, this homogenization would be expected to improve tumor oxygenation.

The first two columns of Panel 2D show MTT and CTH derived from the pre- and post-treatment transit time distributions in Figure 2C. As transit time distributions were experimentally determined in this case, we determined the OEF\textsuperscript{max} values shown in the third column using Equation 1 in Ref. (20), rather than assuming a gamma variate distribution. We assumed identical tissue oxygen tensions (P\textsubscript{tO2}) of 7.5 mmHg for all three conditions. Note that in this tumor type, treatment with SU11657 caused \textit{hemodynamic} vascular normalization in the sense that CTH was reduced in a dose-dependent manner. The parallel reductions in MTT, which were the result of reductions in CBV and increased TBF, however, resulted in a predicted reduction in OEF\textsuperscript{max}. The net oxygenation, TMRO\textsubscript{2}^\text{max}, is given as the arterial oxygen concentration multiplied by TBF and OEF\textsuperscript{max}. Note that tumor oxygenation \textit{increased} in the high-dose condition as a net effect of an increase in TBF (23) that outweighed the reduction in OEF\textsuperscript{max}, but \textit{decreased} in the low dose experiment. The example underscores the importance of knowing the treatment-related changes in MTT and CTH in order to predict how the availability of oxygen in a given tumor is affected by various doses of anti-angiogenic therapy.

Abbreviations: arbitrary units (a.u.); tumor blood flow (TBF); transit time heterogeneity (CTH), mean transit time (MTT); tissue oxygen tension (P\textsubscript{tO2}); capillary blood volume (CBV); maximum achievable oxygen extraction fraction (OEF\textsuperscript{max}); maximum tumor metabolic rate of oxygen (TMRO\textsubscript{2}^\text{max}).
Figure 3. The relation between MTT, CTH, tumor oxygen tension, and the extraction efficacy and net availability of oxygen and glucose in tumors

Panels 3A and 3B show model predictions of OEF_{max} and TMRO_2^{max} in a tumor model for which TBF and resting metabolism values were available for model calibration – See Table 1 in Ref. (26). We chose xenografted breast carcinoma grown to a size of around 2.5 g (35±1 days) in mice, for which TBF = 16 mL/100 mL/min, TMRO_2 = 1.18 mL/100mL/min, OEF = 0.46. To calibrate the model parameter \( k \) for oxygen, we assumed P_{tO2} to be 7.5 mmHg, and set CBV to 3 mL/100mL (corresponding to MTT = 11.25 sec) and CTH to 95% of MTT under these conditions. The arterial blood oxygen concentration was set to 0.185 mL/mL. The OEF_{max} value that corresponds to a given location in the (MTT, CTH) plane is best inferred from the OEF_{max} values indicated on the two nearest solid EF_{max} iso-contours. Note that increases in CTH always reduce the EF_{max} of oxygen for a fixed MTT (or TBF) and tissue oxygen tension. Note that for combinations of MTT and CTH above the yellow dashed line in panel 3B, incremental increases in TBF (reductions in MTT) no longer improves tumor oxygenation. As shown by the arrows, the improvement of tumor oxygenation by elevating TBF is contingent on the simultaneous homogenization of capillary flows to reduce the effective shunting of blood at high CTH values.

We calculated the corresponding values for glucose, assuming TMR_{glc} = 43μmol/100g/min and EF_{glc} = 0.34 – See Table 1 in Ref. (26). We assumed the tissue concentrations of glucose to be 1.25 mmol/L, and an arterial glucose concentration of 7.76 mmol/L. Panel 3C shows TMR_{glc}^{max}/6 TMRO_2^{max}. When this ratio is unity, the vasculature can support glucose utilization by oxidative phosphorylation. Note how both elevated MTT (low TBF) and elevated CTH owing to tumor angiogenesis, tends to necessitate ATP generation by aerobic glycolysis.
The green surface in panel 3D corresponds to combinations of MTT, CTH, and PtO₂, for which oxygen availability precisely matches the TMRO₂ of the xenografted breast carcinoma in panel 3B (TMRO₂ = 1.18 mL/100mL/min) (26). The interior of the half-cone therefore represents combinations of MTT, CTH and PtO₂ for which this the metabolic needs of this tumor type can be met. The red plane marks the boundary of malignant CTH, to the left of which increased tumor blood flow would reduce tumor oxygenation. Note that as CTH increases, for example at a tissue PtO₂ of 15 mmHg, tumor oxygen metabolism can no longer be supported as CTH reaches the critical limit indicated by a. The model predicts that as CTH increases further, the metabolic needs of the tumor can only be met provided TBF can be suppressed (MTT prolonged) and PtO₂ reduced. The resulting decrease in the degree of shunting and improved blood-tissue concentration gradient permit higher levels of CTH, until oxygenation finally becomes critical as PtO₂ approaches zero.

Abbreviations: Tumor blood flow (TBF); transit time heterogeneity (CTH), mean transit time (MTT); tissue oxygen tension (PtO₂); capillary blood volume (CBV); maximum achievable oxygen extraction fraction (OEF<sup>max</sup>); maximum tumor metabolic rate of oxygen (TMRO₂<sup>max</sup>); measured tumor metabolic rate of oxygen (TMRO₂); measured tumor metabolic rate of glucose (TMRglc); measured extraction fraction of glucose EFglc; measured oxygen extraction fraction (OEF).
Figure 2

A. Normal tissue vasculature

B. Tumor vasculature

C. CTH changes to treatment

D. Model predictions

<table>
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<th>Treatment</th>
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<th>CTH (sec)</th>
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<th>TBF (a.u.)</th>
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Figure 3

A. OEF$^{\text{max}}$ (mL/mL) vs. CTH (sec) and MTT (sec) with regions marked for Decreased CBV, Increased CBV, Angiogenesis, and Chaotic capillary flow patterns.

B. TMRO$_2$ (mL/100mL/min) vs. CTH (sec) and MTT (sec) with marked areas for Increased TBF @ high CTH and Increased TBF and CTH reduction.

C. Glucose:Oxygen uptake ratio / 6 vs. CTH (sec) and MTT (sec) with a region marked for Angiogenesis.

D. $P_{O_2}$ (mmHg) vs. CTH (sec) and MTT (sec) with indicated points a and b showing changes in aerobic glycolysis (Warburg effect).
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